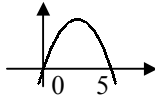


C2 Paper J – Marking Guide

1. (i) $r = \frac{-15}{75} = -\frac{1}{5}$ M1 A1
 (ii) $= \frac{75}{1 - (-\frac{1}{5})} = 62\frac{1}{2}$ M1 A1 (4)

2. $5x - x^2 = 0$
 $x(5 - x) = 0$
 crosses x -axis at $(0, 0)$ and $(5, 0)$ 
- area = $\int_0^5 (5x - x^2) dx$
 $= [\frac{5}{2}x^2 - \frac{1}{3}x^3]_0^5$ M1 A2
 $= (\frac{125}{2} - \frac{125}{3}) - (0)$ M1
 $= 20\frac{5}{6}$ A1 (6)

3. (i) 11 a.m. $\therefore t = 3$
 $N = 20\,000 \times (1.06)^3 = 23820$ (nearest unit) M1 A1
 (ii) $40\,000 = 20\,000 \times (1.06)^t$
 $(1.06)^t = 2$ M1
 $t = \frac{\lg 2}{\lg 1.06} = 11.8957$ M1 A1
 11.8957 hours = 11 hours 54 mins \therefore 7.54 p.m. A1 (6)

4. (i)

x	2	3	4	5	6
y	2.89	6.36	11.55	18.50	27.27

 B2
- (ii) area $\approx \frac{1}{2} \times 1 \times [2.89 + 27.27 + 2(6.36 + 11.55 + 18.50)]$ B1 M1
 $= 51.5$ (3sf) A1
- (iii) over-estimate B1
 the curve passes below the top edge of each trapezium B1 (7)

5. (i) $\sin^2 \theta = (2 - \sqrt{2})^2 = 4 - 4\sqrt{2} + 2 = 6 - 4\sqrt{2}$ M1
 $\cos^2 \theta = 1 - (6 - 4\sqrt{2}) = -5 + 4\sqrt{2}$ M1 A1
- (ii) $3x = \frac{\pi}{6}, 2\pi - \frac{\pi}{6}, 2\pi + \frac{\pi}{6}$ B1 M1
 $3x = \frac{\pi}{6}, \frac{11\pi}{6}, \frac{13\pi}{6}$ A1
 $x = \frac{\pi}{18}, \frac{11\pi}{18}, \frac{13\pi}{18}$ M1 A1 (8)

6. (i) isosceles $\therefore \angle AMB = 90^\circ$
 $BM = 4 \tan 30^\circ = \frac{4}{\sqrt{3}}$ M1 A1
 area = $\frac{1}{2} \times 8 \times \frac{4}{\sqrt{3}} = \frac{16}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = \frac{16}{3}\sqrt{3}$ cm² M1 A1
- (ii) area of sector = $\frac{1}{2} \times 4^2 \times \frac{\pi}{6} = \frac{4}{3}\pi$ B1 M1
 shaded area = $\frac{16}{3}\sqrt{3} - (2 \times \frac{4}{3}\pi)$ M1
 $= \frac{16}{3}\sqrt{3} - \frac{8}{3}\pi = \frac{8}{3}(2\sqrt{3} - \pi)$ cm² A1 (8)

7.	(i)	$= 2^4 + 4(2^3)(x) + 6(2^2)(x^2) + 4(2)(x^3) + x^4$ $= 16 + 32x + 24x^2 + 8x^3 + x^4$	M1 A1 B1 A1
	(ii)	$(2-x)^4 = 16 - 32x + 24x^2 - 8x^3 + x^4$ $(2+x)^4 + (2-x)^4 = 32 + 48x^2 + 2x^4, \quad A = 32, B = 48, C = 2$	M1 A1
	(iii)	$32 + 48x^2 + 2x^4 = 136$ $x^4 + 24x^2 - 52 = 0$ $(x^2 + 26)(x^2 - 2) = 0$ $x^2 = -26$ (no real solutions) or 2 $x = \pm\sqrt{2}$	M1 A1 A1 (9)

8.	(i)	$y = \int (3 - \frac{2}{x^2}) dx$ $y = 3x + 2x^{-1} + c$ $(2, 6) \therefore 6 = 6 + 1 + c$ $c = -1$ $\therefore y = 3x + 2x^{-1} - 1$	M1 A2 M1 A1 A1
	(ii)	$\int_2^3 (6\sqrt{x} - \frac{4}{\sqrt{x}}) dx = [4x^{\frac{3}{2}} - 8x^{\frac{1}{2}}]_2^3$ $= [4(3\sqrt{3}) - 8\sqrt{3}] - [4(2\sqrt{2}) - 8\sqrt{2}]$ $= (12\sqrt{3} - 8\sqrt{3}) - (8\sqrt{2} - 8\sqrt{2})$ $= 4\sqrt{3} \quad [k = 4]$	M1 A2 M1 B1 A1 (12)

9.	(i)	$f(-1) = r \therefore -1 + k + 7 - 15 = r$ $k = r + 9$ $f(3) = 3r \therefore 27 + 9k - 21 - 15 = 3r$ $3k = r + 3$ subtracting, $2k = -6$ $k = -3$	M1 A1 M1 M1 A1
	(ii)	$r = -3 - 9 = -12$	B1
	(iii)	$f(x) = x^3 - 3x^2 - 7x - 15$ $f(5) = 125 - 75 - 35 - 15 = 0 \therefore (x - 5)$ is a factor	M1 A1
	(iv)	$\begin{array}{r} x^2 + 2x + 3 \\ x-5 \overline{) x^3 - 3x^2 - 7x - 15} \\ \underline{x^3 - 5x^2} \\ 2x^2 - 7x \\ \underline{2x^2 - 10x} \\ 3x - 15 \\ \underline{3x - 15} \\ 0 \end{array}$ $\therefore (x-5)(x^2 + 2x + 3) = 0$ $x = 5$ or $x^2 + 2x + 3 = 0$ $b^2 - 4ac = 2^2 - (4 \times 1 \times 3) = -8$ $b^2 - 4ac < 0 \therefore$ no real solutions to quadratic \therefore only one real solution	M1 A1 M1 A1 (12)

Total **(72)**